Micro- and Macrorheological Properties of Isotropically Cross-Linked Actin Networks

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ABSTRACT Cells make use of semiflexible biopolymers such as actin or intermediate filaments to control their local viscoelastic response by dynamically adjusting the concentration and type of cross-linking molecules. The microstructure of the resulting networks mainly determines their mechanical properties. It remains an important challenge to relate structural transitions to both the molecular properties of the cross-linking molecules and the mechanical response of the network. This can be achieved best by well defined in vitro model systems in combination with microscopic techniques. Here, we show that with increasing concentrations of the cross-linker heavy meromyosin, a transition in the mechanical network response occurs. At low cross-linker densities the network elasticity is dominated by the entanglement length $l_c$ of the polymer, whereas at high heavy meromyosin densities the cross-linker distance $l_m$ determines the elastic behavior. Using microrheology the formation of heterogeneous networks is observed at low cross-linker concentrations. Micro- and macrorheology both report the same transition to a homogeneous cross-linked phase. This transition is set by a constant average cross-linker distance $l_m \approx 15 \mu m$. Thus, the micro- and macromechanical properties of isotropically cross-linked in vitro actin networks are determined by only one intrinsic network parameter.

INTRODUCTION

The proper functioning of living cells relies on the tight control of their local viscoelastic properties. Cells achieve this by the dynamic regulation of their cytoskeletal structures. To obtain a quantitative physical understanding of how the network microstructure correlates with the viscoelastic response, in vitro reconstituted networks have been proven to be crucial (for a recent review, see, e.g., Bausch and Kroy (1)). In this respect, the semiflexible polymer actin has drawn much attention in recent years. The elastic response of solutions of actin filaments can be best understood in terms of confinement by surrounding polymers (2,3). In contrast, the mechanics of cross-linked networks seem to depend much more on single polymer properties (4,5). Moreover, depending on the molecular structure of the cross-linking molecules, different actin networks are formed. Actin binding proteins (ABPs) such as filamins (6,7) or scrum (8) organize actin filaments into composite phases, whereas the ABPs fascin (5) and espin (9) as well as depletion forces (10,11) enable the formation of purely bundled networks. Only with heavy meromyosin (HMM) in the rigor state can a purely isotropically cross-linked network be obtained for a broad range of ABP concentrations, which allows theoretical predictions to be thoroughly tested (12). The static linear macroscopic response of isotropically cross-linked networks can be fully explained by a single filament model (4), whereas the frequency dependence of the loss modulus is determined by the unbinding kinetics of the cross-linkers (12). In these networks the nonlinear elastic response is highly nonuniversal and dominated by unbinding events of cross-linking molecules. The linear elastic network response is determined by only one length scale, which is the average distance between cross-linkers $l_m$. Thus, homogeneously cross-linked actin networks are ideally suited to test the sensitivity of microrheological techniques on characteristic network length scales (13,14).

Here, we show that the viscoelastic response of isotropically cross-linked actin networks is determined by the intrinsic network parameter $l_m$, both on the macroscopic and the microscopic scale. Two distinct regimes in the mechanical response can be distinguished: For very low HMM concentrations, the confinement of single filaments by neighboring polymers is sufficient to rationalize the obtained scaling behavior of the plateau modulus $G_0$ as a function of HMM concentration. At high cross-linker densities the affine stretching of single filaments dominates the linear elastic network response. The transition between both regimes is set by the cross-linker distance $l_m \approx 15 \mu m$, which is on the order of the persistence length of actin filaments. Cross-linker-induced heterogeneities are identified for the low HMM concentration regime using microrheology. With increasing cross-linker concentration the relative network heterogeneity decreases until the critical cross-linker distance $l_m \approx 15 \mu m$ is reached. At even higher HMM concentrations the relative distribution width of the local elastic modulus remains constant. With decreasing $l_m$, micro- and macrorheological techniques give converging results even in absolute numbers underlining the length dependence of microrheology.

MATERIALS AND METHODS

Proteins

G-actin is obtained from rabbit skeletal muscle and stored in lyophilized form at $-21^\circ C$. G-actin solution is prepared by dissolving lyophilized
actin in deionized water and dialyzed against G-buffer (2 mM Tris, 0.2 mM CaCl₂, 0.2 mM DTT, and 0.005% NaN₃, pH 8.0) at 4°C. The G-actin solution is kept at 4°C and used within 7 days. Gelsolin from bovine plasma serum is used to adjust the average filament length to 21 μm (16). Polymerization is initiated by adding 1/10 vol of 10× F-buffer (20 mM Tris, 20 mM MgCl₂, 2 mM CaCl₂, 1 M KCl, and 2 mM DTT, pH 7.5) and gently mixing for 10 s. HMM is prepared from myosin II obtained from rabbit skeletal muscle following the literature (17,18). Its functionality was tested using standard motility assays (19). Actin networks with distinct amounts of HMM (heavy meromyosin) are investigated, tuning the molar ratio $R_{\text{HMM}}/c_{\text{actin}}$ over three decades from 0 to 1/50. For all samples the time dependence of the moduli is observed before measurements. This ensures that all ATP is depleted and HMM motor activity is arrested in its rigor state.

**Macrorheology**

The viscoelastic response of actin/HMM networks is determined by measuring the frequency-dependent viscoelastic moduli $G'(\omega)$ and $G''(\omega)$ with a stress-controlled rheometer (Physica MCR 301; Anton Paar, Graz, Austria) within a frequency range of three decades. Approximately 500 μl sample volume is loaded within 1 min into the rheometer using a 50-mm plate-plate geometry with 160-μm plate separation. To ensure linear response only small torques (~0.5 μN m) are applied. Actin polymerization is carried out in situ; measurements are taken 60 min after the polymerization is initiated.

**Microrheology**

A magnetic tweezer microheometer equipped with phase contrast microscopy is used to obtain local information on the viscoelastic moduli (20–22). The maximum force applicable with our setup is 5 pN, limiting the use of this technique to materials softer than ~10 Pa. The viscoelastic moduli at a frequency of 0.1 Hz are determined at various positions in the sample; frequency spectra are taken within a frequency range of two to three decades depending on the sample stiffness. Approximately 20 μl sample volume is loaded into a cuvette, covered with a glass slide, and sealed with vacuum grease. Although the position of the magnetic coils is fixed with respect to the objective, the cuvette holder can be displaced. This ensures that all observed particles are placed in the center of the magnetic coils. This facilitates the microheometer calibration, which is conducted in glycerol saturated with CsCl, Monodisperse paramagnetic beads (4.5 μm in diameter, Dynal M-450; Invitrogen, Karlsruhe, Germany) are added before polymerization and used as probing particles.

**RESULTS AND DISCUSSION**

In the rigor state HMM organizes an entangled actin solution into an isotropically cross-linked network (12). At low concentrations of HMM, $(R_{\text{HMM}}/c_{\text{actin}} < 1/2000)$, the macroscopic viscoelastic network response is similar to that of an entangled actin solution. Thus the elastic response can be understood in terms of deformation of reptation tubes. The frequency spectrum of the viscoelastic moduli is highly similar to the frequency behavior of an entangled actin solution (Fig. 1). Above a critical concentration $R_{\text{macro}}^c$ $(R > 1/2000)$ the shape of the frequency spectra is significantly changed and the elastic response becomes very sensitively dependent on the HMM concentration: a pronounced plateau appears in the storage modulus $G'$ whereas the loss modulus $G''$ exhibits a minimum at low frequencies for samples with $R > 1/1000$. This minimum in $G''$ is a signature of unbinding events of single cross-linkers occurring in the network (12). However, a minimum in $G''$ is not observable at low $R$ within the frequency range probed.

To quantify this mechanical transition at $R_{\text{macro}}^c$ the plateau modulus $G_0$ is determined at the minimum position in the loss modulus for distinct HMM concentrations. This is done for two different actin concentrations ($c_a = 0.4$ mg/ml and $c_a = 0.8$ mg/ml) as depicted in Fig. 2. Two distinct regimes of mechanical response are observed in the first regime. $G_0$ is almost independent of the HMM concentration, showing a scaling of $G_0 \sim R^0$. The observed dependence on the polymer density, $G_0 \sim c_a^{1.3}$, is in good agreement with predictions.
from the tube model for entangled actin solutions (2). Thus, at very low HMM densities a theoretical description based on the tube model holds—similar to observations for networks cross-linked by other actin-binding proteins as, e.g., fascin (5) or α-actinin (23). In the second regime, \( G_0 \) is strongly dependent on the HMM concentration: \( G_0 \sim R^{1.2} \). This agrees well with former findings on densely cross-linked HMM networks. Moreover, the dependence on the actin concentration as predicted by an affine stretching model (12,4) is reproduced, \( G_0 \sim c^2 \). These different scaling regimes cross over at a critical molar ratio \( R_{\text{macro}}^* \), which is only slightly dependent on the actin concentration (\( R_{\text{macro}}^* = 1/2000 \) for \( c_a = 0.4 \text{ mg/ml} \) and \( R_{\text{macro}}^* = 1/5000 \) for \( c_a = 0.8 \text{ mg/ml} \)). Only by determining the concentration dependencies in both regimes can the critical molar ratio where the transition occurs be determined precisely.

To shed some light on the micromechanical origin of the transition in the macroscopic network response, local measurements of the network elasticity are performed using active microrheology (20). Qualitatively, the \( G' \) and \( G'' \) frequency spectra obtained by microrheology exhibit the same transition in the overall shape as observed in macro-rheology (Fig. 3). The transition point \( R_{\text{micro}}^* = 1/2000 \) obtained from microrheology agrees very well with the mechanical transition point \( R_{\text{macro}}^* \) determined by macro-rheology. This suggests that the observed mechanical transition is guided by an intrinsic network length scale on the order of several microns because microrheology is sensitive to such small length scales.

For a detailed statistical analysis of putative local heterogeneities, the viscoelastic moduli are determined at various positions in the sample (~100 positions per sample) for an intermediate frequency (0.1 Hz). From the distribution data of \( G'(0.1 \text{ Hz}) \) cumulative probabilities are calculated for different \( R \) (Fig. 4 A). Also in the form of the distributions two regimes can be distinguished: below \( R_{\text{micro}}^* \) the distribution curves show the occurrence of pronounced heterogeneities whereas above the critical concentration \( R_{\text{micro}}^* = 1/2000 \) homogeneous distributions are obtained. In the latter, the mean values and the absolute widths of the distributions increase with increasing cross-linker concentration \( R \). Thus, normalizing the cumulative probabilities by their respective average elastic modulus (Fig. 4 B) results in a collapse onto a single curve. Interestingly, this normalized distribution curve is identical with the distribution curve obtained for an entangled actin solution, nicely confirming the homogeneous and isotropic cross-linking effect of rigor-HMM (12).

The relative distribution width is given by the normalized standard deviation \( \sigma_{\text{rel}} = \sigma / \langle G'(0.1 \text{ Hz}) \rangle \). A relative width of \( \sigma_{\text{rel}} \approx 20\% \) is obtained for an entangled actin solution as well as for cross-linked networks \( (R > R_{\text{micro}}^*) \) as depicted in the inset of Fig. 4 B. At low HMM concentrations \( (R < R_{\text{micro}}^*) \), \( \sigma_{\text{rel}} \) is more than twice as large corresponding to the broad shape of the distribution curves: the degree of heterogeneity is increased by the addition of a few cross-linking molecules, until at the transition point \( R_{\text{micro}}^* \), a homogenous microstructure is reached again.
The $G'$ distributions obtained for the two lowest ratios ($R = 1/5000$ and $R = 1/10,000$) contain values even lower than the elastic modulus of an entangled actin solution; the corresponding $G'$ histogram exhibits a second peak at $G'(0.1 \text{ Hz}) \approx 20 \text{ mPa}$. At the same time, only very few values exceed the elastic modulus obtained for $R = 0$. To elucidate the network microstructure responsible for this peculiar broadening, full frequency spectra are determined at different sample positions. All obtained spectra have comparable shapes, none of them exhibits a minimum in $G'(\omega)$ within the frequency range probed. Because a minimum in $G'(\omega)$ would be a signature of a cross-linked network, this suggests that in this concentration regime the viscoelastic response is determined rather by local filament density fluctuations induced by the few HMM molecules present than by a formation of cross-linked microdomains, as suggested for $\alpha$-actinin (23).

To elucidate the important network length scales that are responsible for the distinct mechanical scaling regimes we compare the macrorheological results with the local magnetic tweezer measurements. The frequency behavior of $G'$ and $G''$ is determined at distinct positions in the cross-linked network using active microrheology. The resulting frequency spectra are averaged to obtain a quantity that represents the frequency-dependent response of the whole network—although locally measured. $G_0$ is determined as described before and compared to the macroscopic results as depicted in Fig. 5. The same $R^*$ is obtained from these two techniques. Although below $R^*$ the microscopic modulus is approximately a factor of 3–4 lower compared to the macroscopic value, both measurements agree better and better with increasing $R$. Finally, both curves merge at $R^* = 1/100$ as can be clearly seen from the inset of Fig. 5, which depicts the direct ratio $\zeta = G_{0\text{macro}}/G_{0\text{micro}}$ in dependence of $R$. It is important to note, that for the low $R$ samples showing the broad distributions in the microscopic modulus the disagreement between the micro- and macrorheological measurements is most pronounced, $\zeta \approx 4$. Although for the entangled actin solution $\zeta \approx 2.5$, this ratio decreases down to $\zeta \approx 1$ at $R^* \approx 1/100$. Beyond $R^*$ both techniques report the same absolute values for the plateau modulus $G_0$, indicating that both moduli obtained by the micro- and macrorheological techniques are determined by the same mesoscopic length scale.

For a semiflexible polymer network the mechanical response crucially depends on the length scale probed. Therefore, it would be desirable to correlate both experimentally determined parameters $R^*$ and $R^*$ to intrinsic network length scales. For an isotropically cross-linked network the dominating length scale is the cross-linker distance $l_c$, which can be determined by the onset of the nonlinear regime. The elasticity of the network should become nonlinear at large strains with decreasing $l_c$. Nonlinear effects will set in at a critical deformation $\gamma_{\text{crit}}$ from which $l_c$ can be calculated. For isotropically cross-linked HMM networks it was experimentally shown that $l_c$ is given by $l_c = 1.6 \times l_p \times \gamma_{\text{crit}}$ (12), which is in agreement with a linear stretching model.

Therefore, the parameter $R^*$ describing the transition from the regime dominated by entanglements to the cross-linked regime can now be physically understood: the crossover from one scaling regime to the other occurs at well-defined $l_c$, which is approximately constant within the error bars ($17 \pm 2 \mu\text{m}$ for $c_a = 0.4 \text{ mg/ml}$, $14 \pm 2 \mu\text{m}$ for $c_a = 0.8 \text{ mg/ml}$). $G_0$ can be parameterized in the two distinct scaling regimes in a similar way as done for the bundle transition observed for fascin networks ((5); see Appendix for details). By this way, a constraint relating $R^*$ to the actin concentration is obtained, as $R^* \propto c_a^{-6/5}$. Introducing the entanglement length $l_e \sim c_a^{-2/5} \times l_p^{1/5}$ results in the relation $c_{\text{HMM}} \times l_e^{1/2} \approx \text{const.}$ describing the transition line depicted in Fig. 2 (dashed line).

As it turns out, with increasing actin concentration (corresponding to decreasing $l_c$) only smaller amounts of HMM molecules are necessary to induce the crossing over to the second scaling regime. Thus, the critical parameter that is held constant along the "phase boundary" is nothing else than the average cross-linker distance $l_c$ because no overall rearrangement in the network structure occurs. One might speculate that $l_c \sim 14–17 \mu\text{m}$ could refer to the percolation threshold at which the cross-link density is high enough to evoke an overall network response that is not dominated by entanglements anymore. This in turn is set by the persistence length—determining the length scale for tube confinement effects. As in the case of HMM networks the overall network structure will not be changed when crossing $R^*$, no extra free energy or enthalpy compensation is needed for structural rearrangements. Thus, less HMM molecules are required to induce the mechanical transition at higher filament densities.

This stands in marked contrast to what was observed for the bundling transition reported for fascin networks (5). In the
latter case the formation of a purely bundled phase will lead to a strong decrease in configurational entropy, which has to be balanced with a sufficient gain in binding enthalpy. Thus, for the bundling transition of fascin networks a qualitative different constraint was obtained, \(c_{\text{fascin}} \times l_c^{-1/2} \approx \text{const.}\)

The parameter \(R^*\), where both the microscopic and the macroscopic measurement technique report the same viscoelastic response in absolute numbers, corresponds to a cross-linker distance of \(l_c \approx 5 \mu \text{m}\). This excellently matches the diameter of the beads used for active microrheology. At this point the bead explores the full spectrum of dominating relaxation modes whereas at larger \(l_c\) (corresponding to lower \(R\)) long-wavelength fluctuations are not fully reported (13). Thus, the plateau modulus will be underestimated, resulting in the observed discrepancy of the microrheological and macro-rheological measurements. In comparison to experiments that were performed on entangled actin solutions (13) it would be expected that this transition point depends on the size of the probing particle and the type of the microrheological technique because two-point microrheology might not show this pronounced dependence on the network length scales.

Still, there remains a small difference between the macroscopic and the microscopic frequency spectrum, even at \(R > R^*\), as the minimum in \(G^*(\omega)\) always occurs at lower frequencies in the case of microrheology. At the same time, the uprise of \(G^*(\omega)\) at even smaller frequencies is more pronounced in the microscopic frequency spectrum. This might be attributable to the fact that a minimum in \(G^*(\omega)\) is a signature of unbinding events occurring at cross-linking points. Because the microrheological technique used in this study is much more sensitive to local changes in the microstructure, one might speculate that unbinding events in the vicinity of the probing particle can be reported much easier using a magnetic tweezer than a macrorheometer.

In conclusion, we have shown that combining active micro- and macro rheology can elucidate the structure-mechanics relation of semiflexible polymer networks. The purely isotropically cross-linked network obtained by adding rigorous HMM to actin solutions has been proven to be a powerful tool to obtain not only a microscopic understanding of the mechanics but also a detailed description of the structural transition induced by the cross-linker molecules. The occurrence of heterogeneities at low cross-linker concentrations may be a more generic phenomenon and a prerequisite for the structural transition into a network dominated by cross-links. Beyond this transition point, however, the networks formed may differ both in structure and viscoelastic response depending on the type of ABP used. In fact, the network microstructure will determine whether affine stretching or nonaffine bending is the dominating deformation mode then. The obtained physical description of the transition between entangled to isotropically cross-linked networks will be indispensable for the more complicated transitions into composite or purely bundled phases as induced by other ABPs.

### APPENDIX: DERIVATION OF THE CONSTRAINT FOR THE PHASE TRANSITION

As depicted in Fig. 2, there are two distinct regimes in the mechanical response of HMM networks. In each regime \(i = 1, 2\) the plateau modulus \(G_0(R, c_\text{a})\) can be parameterized starting from an arbitrary but fixed transition point \(G_0(R^*, c_\text{a})\) by

\[
G_0(R, c_\text{a}) = G_0(R^*, c_\text{a}) \times f_1 \left( \frac{c_\text{a}}{c^*_\text{a}} \right) \times g_1 \left( \frac{R}{R^*} \right).
\]

This is possible since the influence of \(c_\text{a}\) and \(R\) on the plateau modulus is independent from each other. At any transition point (*) the two parameterizations from regime 1 and 2 have to be equal. This leads to the following equation:

\[
f_1 \left( \frac{c_\text{a}}{c^*_\text{a}} \right) \times g_1 \left( \frac{R}{R^*} \right) = f_2 \left( \frac{c_\text{a}}{c^*_\text{a}} \right) \times g_2 \left( \frac{R}{R^*} \right).
\]

The functions \(f_i\) and \(g_i\) can be read from the scaling \(G_0(R)|_{\text{macro}}\) and \(G_0(c_\text{a})|_{\text{macro}}\) because they are experimentally determined to be power laws:

\[
\left( \frac{c^*_\text{a}}{c_\text{a}} \right)^{1.3} \left( \frac{R^*}{R} \right)^{0.1} = \left( \frac{c^*_\text{a}}{c_\text{a}} \right)^{2.5} \left( \frac{R^*}{R} \right)^{1.2}.
\]

This is simplified to

\[
\frac{R^*}{R} = \left( \frac{c^*_\text{a}}{c_\text{a}} \right)^{-6/5} (++)\text{,}
\]

which gives a parameterization for all transition points (dashed line in Fig. 2). To predict the shift of the transition ratio \(R^*\) with respect to \(c_\text{a}\), we apply (++) to two different transition points \((R_1|c^*_{\text{a}1})\) and \((R_2|c^*_{\text{a}2})\) and calculate the ratio of the resulting equations. Thus, the starting point \(G_0(R^*, c_\text{a})\) is cancelled out resulting in \(R^*_1/R^*_2 = (c^*_{\text{a}1}/c^*_{\text{a}2})^{-6/5}\).

By this way a constraint relating \(R^*_\text{macro}\) to the actin concentration is obtained:

\[
R^*_\text{macro} \sim c^{-6/5}.
\]

In the following * is left out, and everything from now on refers to the transition line. Replacing \(R\) by its definition yields:

\[
\frac{c_{\text{HMM,1}}/c_\text{a,1}}{c_{\text{HMM,2}}/c_\text{a,2}} = \left( \frac{c_\text{a,1}}{c_\text{a,2}} \right)^{-6/5} \leftrightarrow c_{\text{HMM,1}} \times c_\text{a,1}^{1/5} = c_{\text{HMM,2}} \times c_\text{a,2}^{1/5} = \text{const.}
\]

Introducing the entanglement length \(l_e \sim c^2/5 \times l_{0,5}^5\) results in the relation given in the manuscript: \(c_{\text{HMM}} \times l_{e,5}^{1/5} \approx \text{const.}\)

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